Pseudo-Random Number Generation

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Abstract

Redshift provides two PRNGs, one on the leader node and one on the worker nodes. The leader node PRNG is correctly implemented. The worker node PRNG is fundamentally flawed. Each worker slice produces a linear, minutely incrementing number sequence (the "non-PRNG number sequence") which cycles between 0.0 and 1.0, where when a query is issued, each slice consumes the current number from that sequence and uses it as the seed for a PRNG, which in turn uses it to generate a random number sequence for and only for that query. The first random number emitted by a query on each slice is the number from the non-PRNG number sequence on that slice. The following numbers are from the PRNG. Low-entropy non-PRNG number sequence numbers, occurring when the numbers contain many zero bits, lead to correlation between the initial numbers produced by a PRNG for a query, and also between the initial values produced between queries.

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Introduction

This paper is an investigation into the pseudo-random number generator (PRNG) in Redshift, and credit here must be given to another software engineer.

I began to investigate this subject in early 2021, but was immediately directed by a fellow Redshift admin to a post on the official Amazon Redshift Developer Forums, made by Murat Tasan (LinkedIn), which describes major design flaws in the PRNG.

The origin of the investigation in this paper is his findings, which I have investigated, determined the causes, formalized with a script to provide reproducibility, and then extended by investigating further aspects of behaviour in different situations.

In general, then, this white paper explores the behaviour of the pseudo-random number generators (there's more than one, as you will see) in Redshift.

Redshift Internal Architecture

This white paper intended to explore random number generation, then in doing so ran into what I think is a change made something like a year ago in the internal architecture of Redshift, and which I've been observing in various places since then but have yet to actually investigate.

Note though this is based on my recollections of behaviour prior to this time, as I have no earlier investigations into this matter, so I can't compare what happens now with a formal record of what used to happen - so I could be wrong.

Nevertheless, the crux of this change, as I understand it, must be described in this white paper, and at this point, for without it the white paper will make no sense at all - even the test methods cannot be explained - even though here in this paper I am not providing proofs.

So, turning to the subject in hand: when it comes to Redshift clusters, it is never possible to run older versions. You can only run what's available now (and maybe one previous release). So I can always exactly determine what Redshift does *now*, but for anything in the past where I lack formal proofs, I'm relying on memory.

I think I remember things were different - but having no formal records of this behaviour, I can't be certain, so there is a possibility here of error on my part.

So, having said that, what I think is this: that it used to be each slice held a portion of the rows in each normal Redshift table, and that only the slice holding the rows could directly access those rows. For other slices to access those rows, the owning slice would need to read them, and then transmit them over the network, as part of the actual work being performed by a query (a broadcast or distribute step).

As such, if a block was stored on a slice and you accessed that block, it would necessarily be that slice which read that block.

Well, to quote Mr. Dylan, "things have changed".

Now, I've not actually sat down and investigated what's going on, so what I relate now are the behaviours I've noticed as I've been doing other work and especially with the investigation work for this white paper.

The key change is that it looks now that every slice on a node can directly access the rows of every other slice on that node.

As such, when a query is issued, say for example a query which uses rows only held by one slice, it is no longer possible to know which slice that query will execute upon; it could execute on any of the slices in that node.

If only one slice on a node holds blocks for a table, there seems to be a strong preference for a query to execute on that slice. If all slices on a node hold blocks, it seems query distribution is pretty evenly spread.

Most queries of course execute on all slices, and in that, the usual case, it won't matter (assuming that slices are wholly symmetric in performance), but here in this white paper for example, with random number generation investigation, I need to ensure queries are running on the same single slice, always. Before, I could do this, by controlling which slice blocks went to and then issuing queries which used blocks on a single slice only. Now I cannot - what I now do in fact is loop over each query until it executes on the slice I want it to execute on. As with certain other changes in recent years (auto-vacuum, system tables becoming views and the underlying tables no longer being accessible, etc), this obstructs investigation.

I suspect this change relate to another change, which occurred between between 2019-09-27 and 2020-10-03 (I have partial dumps of the system tables' DDL and SQL on those dates). We can observe between these times a new column was added to STV_SLICES, type, which is a char(1) where the value is either C or D, which we reasonably can assume mean 'compute' and' data', respectively.

I've only ever been able to get compute slices to show up on ra3 type nodes, and they are brought into existence by an elastic resize.

(Brief refresher on elastic resize: the number of slices remains the same, but the number of nodes changes, and the slices are redistributed over the nodes. So if you add nodes, you end up with more hardware, but less slices per node, and so reduced chances for efficiency by exploiting parallelism. If you remove nodes, you have less hardware, and so save money, but now have more slices on each node, and if you do that too much, the overheads involved in each slice begin to be unduly costly. Modus omnibus in rebus.)

Here's STV_SLICES from a brand new two node ra3.xlplus;

node	1			localslice		type	
	-+-		+-		+-		
0		0	1	0		D	
0		1		1		D	
1	1	2	1	0		D	
1		3	1	1		D	

And this is what we see after an elastic re-size to four nodes.

				localslice		0 1
	:	0	:	0	•	
0		4		1		C
1		2		0		D

1	1	5		1		С
2	1	1	1	0		D
2	1	6	1	1		С
3	1	3	1	0		D
3	1	7	1	1	Τ	С

The number of nodes has doubled, the data slices have been distributed between them, and the other slice on each node is a compute slice.

Compare this to the same re-size for a two node dc2.large;

node				localslice		0 1
0	1		Ċ	0		
0	•	1	•	1	•	
1	İ	2	İ	0	İ	D
1	1	3		1		D

And after a re-size to four nodes;

				localslice		V -
0	:		:	0	Ċ	
1	•	2	•	0	•	_
2	i	1	i	0	i	D
3	1	3	١	0	I	D

Here we see the number of slices remains the same.

This new behaviour is immediately interesting in one way, in that I think it solves, for ra3 nodes, a drawback (as ever, undocumented) with elastic re-size, which is that you get a maximum of ten Redshift Spectrum workers per slice, so if you performed an elastic re-size, you'd be paying for more nodes but you wouldn't be getting more throughput with Redshift Spectrum, because the number of slices was fixed. Now we see elastic re-size actually giving more slices, at least on ra3 - it doesn't on the other node types, not as far as my brief investigation into re-sizing has found.

Speculatively, I would guess the compute slices have no SSD storage of their own. They're on the same node, though, so it doesn't matter now; they can directly access to the blocks held by other slices.

One obvious question is if there are performance issues.

My gut feeling is that only one slice at a time can access the blocks held by a slice. This is something in particular I will look into when I investigate all this new behaviour.

So, finally coming back now to this white paper, where random number generation is investigated, this is why there are in the Python script used to generate evidence loops around queries, which check to see the slice the query executed upon, to ensure results are only from queries which executed on a given slice.

Test Method

There are basically two types of test in this white paper.

The first type of test produces only a few numbers from the PRNG, and presents them in a table, along with an explanation of what they must mean.

The second type produces an *image*, a small grey-scale bitmap, 256 by 256 pixels in size, by converting each random number to a grey-scale pixel; Redshift emits random numbers between 0.0 and 1.0, where 0.0 becomes black and 1.0 becomes white.

A reference image is generated using the Python 3.7.3 PRNG, which I understand is a Mersenne Twister, which is about the best non-cryptographic PRNG out there, and very nice it is too.

The use of an image is a rough and ready method to check if a PRNG is emitting random numbers; if it is not, patterns can be seen in the bitmap. *Any* patterning visible to the plain human eye means the PRNG is emitting garbage.

To properly test a random number generator, pseudo or real, a large battery of statistical tests are performed on its output, and one utility for this is a command line tool known as dieharder.

This is available on my Debian system from the Debian repository, but it's not necessarily available on other systems, and so although I have included in Appendix C its results on the Python 3.7.3 PRNG, the leader-node PRNG and a worker node slice PRNG (the leader node has a different PRNG to the worker nodes), I have not used it generally, since the script which produces evidence for each white paper is specifically intended to be used by readers, so they can verify the results are true for their system, and to check in the future if the results are still true or if Redshift has changed.

Turning directly now to the tests, note all tests on a worker node are run, unless specifically indicated otherwise, on node 0 slice 0. All tests check that their queries actually did run on that slice, and run them again (resetting the seed, of course), if they did not.

All tests are usual are issued on a newly spun-up cluster. For my run of the script, I used a two node dc2.large cluster.

The tests are:

1. Five queries are issued, which produce one row each, with one random number per row, on the leader node.

- 2. One query is issued, which produces five rows, with one random number per row, on the leader node.
- One query is issued, which produces one row, with five random numbers, on the leader node.
- 4. We now check if the PRNG seed/number sequence, on the leader node, is per-session or across all sessions. This is done by opening two connections to the cluster and setting the seed on both to 0, then issuing one query on the first connection taking one row of three random numbers from the leader node, and then the same query, but on the second connection.
 - If the three random numbers are the same for both queries, the seed must be per-session.
- 5. For information purposes, this test generates the first five random numbers from each worker slice.
- 6. We then repeat the previous test, but now with a superfluous query, which does not generate random numbers, between every query.
- 7. One query is issued, which generates five rows, with one random number per row, on worker slice 0.
- 8. Five queries are issued, generating one row each, with five random numbers per row, on worker slice 0.
- 9. One query is issued, with one row, which has one random number per slice, with the query generating one row on each slice.
- 10. We now check if the PRNG seed/number sequence, on the worker node, is per-session or across all sessions. This is done by opening two connections to the cluster and setting the seed on both to 0, then issuing one query on the first connection taking one row of one random number from the leader node, and then the same query, but on the second connection.
 - If the random numbers are the same for both queries, the seed must be per-session.
- 11. This test generates a bitmap of the results from a single query, generating all rows, where each row has a single random number, on the leader node.
- 12. This test generates a bitmap of the results from a single query, generating all rows, where each row has a single random number, on worker slice 0.
- 13. This test generates a bitmap of the results from a 2^16 queries, generating one row each, where each row has a single random number, on the leader node.
- 14. This test generates a bitmap of the results from a 2^16 queries, generating one row each, where each row has a single random number, on worker slice 0.
- 15. This test generates a bitmap of the results from a 2^16 queries, generating one row each, where each row generates five random numbers, on worker slice 0.

- 16. This test generates a bitmap of the results from a (2^16)5 queries, generating one row each, where each row generates five random numbers, on worker slice 0; the bitmap is generated from the second* random number from each query. This demonstrates cross-query correlation.
- 17. This test generates the first five random numbers from worker slice 0, and then generates the same random numbers again except that this second set is generated repeatedly until exactly one of the numbers, between the second and second-to-last, slice hops. The two sets of results demonstrate what happens to the number sequence when slice hopping occurs.

Results

The results are given here for ease of reference, but they are also presented, piece by piece along with explanation, in the Discussion, and it is there you should read about them to understand them.

See Appendix A for the Python pprint dump of the results dictionary.

Download random_number_generation.py, the script used to generate the evidence for this white paper.

 $Usage: ./pseudo_random_number_generation.py one-shot$

The script works in eu-central-1, creates a VPC, configures everything that needs, runs the cluster specified in the test, executes the tests, and dumps the results on screen, then cleans everything up.

The script, like all ARRP scripts, requires boto3 version 1.17.34 or later.

Note this script, where it generates images, makes a directory named images, which it populates, and requires numpy to be installed; I have no idea which version introduced the image generation functionality I'm using. I should think anything non-archaic will be fine.

Total script execution time, including cluster bring-up and shut-down, was $4{,}792$ seconds.

dc2.large, 2 nodes (1.0.30840)

Five Queries, One Row Each, One Number per Row, Leader Node

Query	Number
1	0.840187716763467
2	0.394382926635444
3	0.783099223393947
4	0.798440033104271
5	0.911647357512265

One Query, Five Rows, One Number per Row, Leader Node

Row	Number
1	0.840187716763467
2	0.394382926635444
3	0.783099223393947
4	0.798440033104271
5	0.911647357512265

One Query, One Row, Five Numbers per Row, Leader Node

Number #1	Number #2	Number #3	Number #4	Number #5
0.840188	0.394383	0.783099	0.798440	0.911647

PRNG Seed/Number Sequence per-Session or Global, Leader Node

Session	Query	random() #1	random() #2	random() #3
1	1	0.840187716763467	0.394382926635444	0.783099223393947
2	1	0.840187716763467	0.394382926635444	0.783099223393947

First Five Numbers per Worker Slice

Query	Slice #0	Slice #1	Slice #2	Slice #3	
1	0.0000000000	0000 3.3 66925144	2916 38 733850288	583 23.8 007754328	- 74837
2	0.0000895813	3340 9.5 67014725	6256 9 . 4 33939869	917 29.1 008650142	08892
3	0.0001791626	6681 5.3 67104306	95974934029451	251 34.9 009545955	42948
4	0.0002687440	002 20.6 67193888	2938 0.7 34119032	585 40.4 010441768	377004
5	0.0003583253	336 26 .B67283469	62786.1734208613	919 46 .01011337582	211059

First Five Numbers per Worker Slice (with extra query)

Query	Slice #0	Slice #1	Slice #2	Slice #3	
1	0.0000000000	000 3.3 669251442	291 63.8 733850288	583 23 8 00775432874	837
2	0.0001791626	681 5.3 671043069	959 7019 34029451	251 34.9 00954595542	948
3	0.0003583253	36 26 .B672834696	6278 6.1 734208613	919466.0101133758211	059
4	0.0005374880	043 7:2 674626322	2959 7:2 734387776	587 57.1 101312920879	170
5	0.0007166506	72 48:4 676417949	9640 %3 734566939	2556 %.2 01492083547	281

One Query, Five Rows, One Number per Row, Worker Slice $\boldsymbol{0}$

Row	Number
1	0.0000000000000039
2	0.000985394674650
3	0.041631001594613
4	0.176642642542916
5	0.364602248390607

Five Queries, One Row per Query, Five Numbers per Row, Worker Slice $\mathbf{0}$

Number #1	Number $\#2$	Number #3	Number #4	Number #5
0.0000000000000039	90.000985394674650	0 0.04163100159461	30.176642642542916	60.364602248390607
0.000089581334098	5 0.731953177121920	00.872086605317186	60.375548061256342	20.794304826910761
0.000179162668150	00.462920959569189	90.702542209039759	90.574453479969769	0.224007405430914
0.000268744002200	60.193888742016458	80.532997812762332	20.77335889868319	50.653709983951067
0.000358325336263	1 0.924856524463728	8 0.36345341648490	50.972264317396622	20.083412562471221

One Query, One Row, One Number per Slice, Worker Nodes

Slice #0	Slice #1	Slice #2	Slice #3
0.0000000000000039	0.366925144291638	0.733850288583238	0.100775432874837

PRNG Seed/Number Sequence per-Session or Global, Worker Node

Session	Query	random() #1
1	1	0.0000000000000039
2	1	0.000089581334095

Slice Hopping and PRNG Consumption Pinned to Slice 0

Query	Slice	random()
1	0	0.0000000000000039
2	0	0.000089581334095
3	0	0.000179162668150
4	0	0.000268744002206
5	0	0.000358325336261

Unpinned to Slice 0

Query	Slice	random()
1	0	0.0000000000000039
2	1	0.367014725625694
3	0	0.000179162668150
4	0	0.000268744002206
5	0	0.000358325336261

Discussion

We begin with the leader node. Remember that between every test, seed is set back to zero.

First, we issue five queries, each producing one row, with one random number.

Query	Number
1	0.840187716763467
2	0.394382926635444
3	0.783099223393947
4	0.798440033104271
5	0.911647357512265

These random numbers are then the first five numbers in the leader node PRNG sequence.

Next, we issue one query, which produces five rows, each with one random number.

Row	Number
1	0.840187716763467
2	0.394382926635444
3	0.783099223393947
4	0.798440033104271
5	0.911647357512265

Here we see the same five numbers.

We then issue one query, which produces one row, but that row has five columns, each a random number.

Value #1	Value #2	Value #3	Value #4	Value #5
0.840188	0.394383	0.783099	0.798440	0.911647

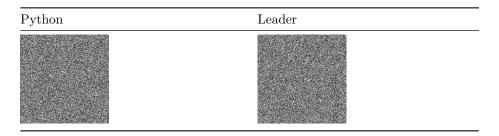
Here again we see the same five numbers.

Finally, we check to see if the PRNG seed/number sequence is per-session, or global across all sessions.

To do this, we open two sessions, set the seed to 0 in both, and issue in both sessions one query which produces one row of three random numbers.

Session #	Query #	random() #1	random() #2	random() #3
1	1	0.840187716763467	0.394382926635444	0.783099223393947
2	1	0.840187716763467	0.394382926635444	0.783099223393947

If the numbers produced from both queries are identical, then the PRNG seed/number sequence must be on a per-session basis, and this is what found.



Here we see the reference bitmap from the Python 3.7.3 PRNG, and the bitmap produced by the leader node PRNG with one query producing all rows, with each row holding one random number. All the variations on generating random numbers (many queries with one row each with each row holding one number, many queries with many rows each with each row holding one number, etc) all produce similar, properly random output.

What we see then is that the leader node PRNG has a single source of random numbers, and every call to random() consumes one number from this sequence, regardless of whether the calls are made over many queries, or many rows per query, or many calls per row. We also see the seed/position in the number sequence is held on a per-session basis.

One of the properties of a PRNG is *reproducibility*, which is to say, that the sequence of numbers produced is always the same, so that once we have picked a starting point in that sequence by setting the seed, we will always get the same sequence of numbers. This is necessary for debugging.

The leader node provides reproducibility.

All in all what we see from the leader node is what we would expect from the leader node, as it was formerly a single-node relational database, and when you only have a single node to deal with, life is much simpler.

Now we turn to worker nodes.

To begin with, we issue *for each slice*, five queries, each producing one row, each row holding one random number. This gives us the first five numbers in the PRNG number sequence for each slice.

Query	Slice #0	Slice #1	Slice #2	Slice #3
1	0.00000000000	0039 0.36692514429	016380.7338502885	832380.100775432874837
2	0.00008958133	4095 0.36701472562	256940.7339398699	172930.100865014208892
3	0.00017916266	8150 0.36710430695	597490.7340294512	513490.100954595542948
4	0.00026874400	2206 0.36719388829	938050.7341190325	854040.101044176877004
5	0.00035832533	6261 0.36728346962	278610.7342086139	194600.101133758211059

What we observe is that each slice, for seed 0, starts at a different location in the number sequence, and that each number being produced is in all cases an increase of 0.000089581334055 on the previous number. When the number exceeds 1.0, it loops back to 0.0.

This is not in fact a PRNG, being from here on referred to as the "non-PRNG number sequence", and so we must now investigate further to find how random number are being generated.

First, if we repeat these queries, but this time issuing after each query a simple select timeofday() from table 1 limit 1, we see that the numbers produced *change*.

Query	Slice #0	Slice #1	Slice #2	Slice #3
1	0.00000000000	0039 0.36692514429	16380.7338502885	5832380.100775432874837
2	0.00017916266	8150 0.36710430695	97490.7340294512	2513490.100954595542948
3	0.00035832533	6261 0.36728346962	78610.7342086139	0194600.101133758211059
4	0.00053748800	4372 0.36746263229	59720.7343877765	5875710.101312920879170
5	0.00071665067	24840.36764179496	40830.7345669392	2556820.101492083547281

In fact, what's happening is the extra query is causing every slice to jump forward by one number in its number sequence, even though the extra query does not generate any random numbers. The second set of results are the same as the first, but with the lines from queries #2 and #4 removed (and the later rows in the second set are not seen in the first set, as both sets only have five rows).

We will come back to this a little later.

Next, if we issue a single query, to worker slice 0, which produces five rows, each with one random number, we see the first number is unchanged, but the succeeding numbers are different to those generated when five individual queries are issued. We are now seeing something new, and which looks more like PRNG output.

Row	Number
1	0.0000000000000039
2	0.000985394674650
3	0.041631001594613
4	0.176642642542916
5	0.364602248390607

This behaviour becomes clearer when we issue five queries, all to slice 0, with seed set to 0 once, at the beginning of the set of five queries, with each query producing one row, where each row has five random numbers.

Number #1	Number #2	Number #3	Number #4	Number #5
0.000000000000039	90.00098539467465	0 0.04163100159461	30.17664264254291	60.364602248390607
0.000089581334098	50.73195317712192	0 0.87208660531718	60.37554806125634	20.794304826910761
0.000179162668150	00.46292095956918	90.702542209039759	90.57445347996976	90.224007405430914
0.000268744002200	60.19388874201645	80.53299781276233	20.77335889868319	50.653709983951067
0.00035832533626	10.92485652446372	80.36345341648490	50.972264317396623	20.083412562471221

First, we see the five random numbers from the first query match the five random numbers produced when we issue single queries which produces one row with one random number each (not the table immediately above with the five columns, but the table above that).

Second, if we look back at the table showing the first five random numbers produced on each slice, we see that the *first* number from each query (remembering the queries here all run on slice 0) is reproducing the first five random numbers from slice 0.

What seems then to be happening is that with the slice begins with the first number in its non-PRNG number sequence (0.00000000000000), and then it generates a sequence of random numbers (the next four random numbers in the row), using a PRNG, derived from that initial number.

Then, when we come to the second query, the slice moves on to the second number in its non-PRNG number sequence (0.000089581334095), and then, as before, the slice generates numbers from a PRNG number sequence derived from that initial number.

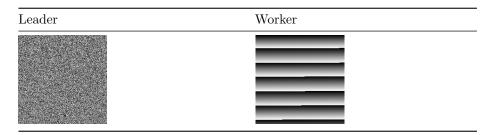
It seems then that every query - and if we think back to the earlier results where we saw queries which were not generating random numbers causing progression down the non-PRNG Number sequence - consumes the current non-PRNG number from the slice(s) it is running on and uses that at the seed for an actual PRNG, to generate the random numbers for that query.

Slice #0	Slice #1	Slice #2	Slice #3
0.0000000000000039	0.366925144291638	0.733850288583238	0.100775432874837

This is what we see here, with a query which generates one row, with one random number per slice. Each slice emits the current number from its own non-PRNG number sequence.

This leads to the immediate observation that any user issuing single queries which produce a single random number is fully exposed to the minutely incrementing non-PRNG number sequence for whatever slice produces the row for that query, because that number is always given as the first random number for a query.

This is a fundamental design flaw; these are not random numbers and random() should provide random numbers no matter how you call it.



On the left, the bitmap produced by the leader node, when we generate pixels by issuing a single query which produces a single row with a single random number. On the right, worker slice 0.

Comparing here the leader node to the worker node is a little unfair, since the leader node is a single computer rather than a cluster and so faces simpler design challenges, but the worker node PRNG can perfectly well be designed so it works correctly, so it's not that unfair.



Figure 1: Unpinned Worker Slice 0

As an aside, figure 1 shows the bitmap produced when no steps are taken to use only numbers generated by slice 0. The speckles mark numbers which were produced on other slices, where their non-PRNG number sequence is different to that on slice 0. Normally I think queries run evenly over slices, but where these numbers are being produced by a select which is using a table which only has blocks on slice 0 (e.g. select slice_num(), random() from table_1 limit 1), there seems to be a strong preference for execution on slice 0.

Designs where a PRNG is seeded from another PRNG are not unknown, but the general advice is that the two PRNGs should use fundamentally different mathematical approaches. In this case, though, there is one non-PRNG number sequence and one PRNG, and this is not going to work correctly.

The problem is superficially ameliorated by each slice being at a different point of the non-PRNG number sequence, but this is a billion miles from being an actual, sound solution; in fact what it does mainly is obscure the problem, which is not what you want.

The reason I think of for a design like this is performance. The idea is that each query only needs to touch the master entropy state once, and then independently produces its own random numbers; if all queries were using the same entropy state to produce all their random numbers you could well end up with quite a bottleneck.

Turning to the secondary PRNG, examination on worker slice 0 demonstrates strong correlation between the initial few numbers created for each query, both simply between themselves but also between the numbers generated by successive queries, where by this I mean to say the first number generated by a query is correlated to the first number generated in the following queries, the second number generated is correlated to the second number generated in the following queries, and so on.

That's not random; random numbers do not correlate to other random numbers, at all, regardless of the query they're in.

Python	Single Query	Cross Query

Here we see a reference bitmap, generated from the Python 3.7.3 PRNG, then a bitmap produced by issuing many queries, which produce one row each, where that row has five random numbers (constructing the bitmap, left-to-right, then top-to-bottom, by concatenating each queries five random numbers), and finally, a bitmap produced by issuing many queries, which produce on row each, where that row has five random numbers, and this bitmap is composed of and only of the *second* random number from each query (and so here to produce a bitmap of the same size, five times as many queries had to be generated; note also the first number from these queries is the non-PRNG number sequence, and so is meaningless, which is why it's not used - we're here looking at the output from the worker slice PRNG, not the non-PRNG number sequence).

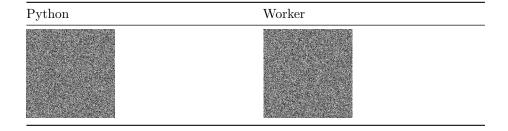
Remember; it may not seem like much, but anything you can actually notice with the plain human eye means output is profoundly broken.

I think the reason for both these problems is that in the test code, where I'm issuing test queries one after the other, the numbers taken from the non-PRNG number sequence are always very similar, and also I suspect being from slice 0, which begins its non-PRNG number sequence almost at zero, have very few bits set and so very little entropy, and it takes the PRNG some iterations to recover from this handicap and get to the point where it's producing decent random numbers.

However, we must note the non-PRNG number sequences loop between 0.0 and 1.0, so all slices will be for extended and contiguous periods be emitting low-entropy numbers.

Aside from this, we must remember that the first number for each query is always non-random, since it is taken from the minutely incrementing non-PRNG number sequence on each slice.

What we see then is that only safe way to use the worker node PRNG is to issue queries which produce enough random numbers to get past the initial non-random numbers. We see here the bitmap produced by worker slice 0 when a single query produces all rows, with one number per row. The first number is not random, as it is the non-PRNG number, then there's a series of low quality random numbers, and then the PRNG gets into its stride. The random numbers produced when worker slice 0 is used in this way perform well in the dieharder tests, the non-random initial numbers being overwhelmed by the many tens of thousands of random numbers which follow.



Here we see the output from worker slice 0 when operated safely.

One thought then when using worker node PRNG is to issue prophylactic calls to random(), to generate the initial non-random or poorly random numbers and throw them away.

We can now turn back to two outstanding questions, whether the seed for worker nodes is per-session or global, and the question of reproducibility.

As before, the test for per-session seed is to make two connections, set seed to zero on both, and then issue a select into each session where the select generates a random number, although with the worker slices we obtain only one random number, rather than the three from the leader nodes (which I did just to show some extra numbers to make things more obvious), because as we've seen, with worker slices random numbers after the first come from the PRNG, which is using the first number as its seed, and so they are purely dependent on the first number and so having the first number is enough.

Session #	Query #	random() #1
1	1	0.0000000000000039
2	1	0.000089581334095

This test demonstrates that the non-PRNG seed/number sequence position is global, not per-session. This means every time any slice moves down the non-PRNG number sequence, all slices do so, throwing away the numbers they skip over.

Query	Slice	random()
1	0	0.0000000000000039
2	0	0.000089581334095
3	0	0.000179162668150
4	0	0.000268744002206
5	0	0.000358325336261

Query	Slice	random()
1	0	0.0000000000000039
2	1	0.367014725625694
3	0	0.000179162668150

Query	Slice	random()
4	0	0.000268744002206
5	0	0.000358325336261

This behaviour combines with slice hopping to produce a rather unexpected outcome. Each slice has its own non-PRNG number sequence, and normally queries which produce a single number will produce that sequence; we see this in the first of the two tables above. However, when a query hops to another slice, and runs there, that query will return a non-PRNG number sequence number from that other slice, and the slice the query normally runs on will move forward by one in its non-PRNG number sequence - permanently throwing away a number, even though we have not consumed it. We see this in the second of the two tables above.

Regarding reproducibility, it is obvious and inherent that Redshift worker nodes do not offer reproducibility.

This is because where Redshift runs on a cluster, reproducibility is in principle problematic. A query will execute, normally, on every slice in the cluster, and there is no telling in which order rows will be produced by the slices; it might be one slice is going slow, or another fast, depending on what other load is at the time present on those slices.

As such, even if the worker node PRNG were producing the same sequence of numbers across all slices, you would still see random numbers turning up in different orders in your rows every time you run a query, because the rows would naturally be generated in different orders every time the query runs.

Finally, note that Murat Tasan, the engineer who noticed the PRNG was behaving very oddly, did so back in December 2016.

That was five years ago. Redshift came out in early 2013, three years before then. My guess is the PRNG has been as it is found now since the beginning.

Conclusions

There are two PRNGs in Redshift; one on the leader node, one on the worker nodes.

The leader node PRNG works correctly, always.

The worker node PRNG is fundamentally flawed.

The worker node PRNG design has each worker node slice producing a linear number series (the "non-PRNG number sequence") where each number is 0.000089581334055 larger than the previous number, where each query, whether it produces random numbers or not, consumes the current number from the non-PRNG number sequence on each slice and uses this as the seed for a per-slice PRNG, which then generates random numbers for that query from the number sequence produced by that seed.

Each query then is generating its own, individual, per-slice sequence of PRNG numbers, where the PRNG is initialized by the number taken from the non-PRNG number sequence on each slice.

The first random number generated by a query, on each slice, is the number taken from the non-PRNG number sequence on that slice. These numbers change very slowly, incrementing each time a query is issued, and so this first number is usually similar or very similar to the previously produced first number; any user issuing consecutive queries which generate random numbers will receive a for their first number on each slice direct copy of the non-PRNG number sequence on each slice.

When queries which generate random numbers are issued in any kind of close succession, the numbers taken from the non-PRNG number sequences are very similar. Those sequences loop between 0.0 and 1.0, in tiny increments, and so for considerable and contiguous periods produce numbers with low entropy many zero bits. When these two events combine, the PRNGs are seeded with numbers which are very similar and low-entropy, and this presents difficulties to the PRNG, which can take a certain number of iterations before it is generating high quality random numbers, and during this time the initial numbers emerging from the PRNG are low quality, such that these numbers are correlated both with themselves (the numbers being generated by a single query) and also with the numbers generated by successive queries.

It is advised then that when using random(), prophylactic calls are made, to generate and then throw away initial low quality random numbers. At the very

least the first random number from each slice must be disposed of, since it is from the non-PRNG number sequence.

The leader node maintains the PRNG seed and number sequence on a persession basis, and provide reproducibility, always generating the same PRNG number sequence for any seed.

The worker nodes maintain the PRNG seed and number sequence globally, over all sessions, although the position of each slice in the number sequence is different. When one slice consumes a number from its non-PRNG number sequence, all slices move down their sequence by one number.

Where the slices in the worker nodes depending on load produce rows at different rates, it is inherently impossible for Redshift to provide reproducibility; even if the PRNG always emitted, across all slices, the same sequence of numbers, where the slices vary in how quickly they produce rows, the ordering of those numbers would always differ between runs of a query.

Unexpected Findings

When you investigate Redshift, there are always unexpected findings.

- 1. I seemed to sometimes run into problems dropping tables which had received large numbers (16,384) of sixteen row single inserts. There would be no queries running, but issuing a drop on the table leads to the drop just sitting there, nothing happening; I had to shut down the cluster. It might be if I waited a long enough time, the drop would work, but I never tried this.
- 2. If you issue a query in a procedure, Redshift will mess with the text you issue, upper-casing the letters of the SQL command and removing any trailing colon. If the query is executed via a cursor, i.e. open cursor for ..., a space is prepended to the query text, but the SQL command is now not capitalized, and in some cases any trailing semi-colon is also removed. Additionally, the text is messed with differently in STL_QUERY compared to STL_QUERYTEXT.
- 3. This may well be a standard PL/pgSQL behaviour, but I've not seen it documented anywhere and it's new to me: opening a cursor with a query does not cause query to execute. You have to call the first fetch to make the query occur.
- 4. In the low-level system tables, such as STL_SCAN, the row count number looks to be off-by-one some of the time. For example, if you scan five rows from pg_class, STL_SCAN reports you scanned six.

Revision History

v1

• Initial release.

$\mathbf{v2}$

• Re-arranged one or two sentences in the internal architecture material, where an old sentence from previous writing had inadvertantly remained in the text.

v3

• Fixed an error in the text where I instructed users to look at another table, but told them the wrong table - I said look up two tables, should have been one.

v4

• No content changes; path to image file(s) changed.

v5

• Changed to Redshift Research Project (AWS have a copyright on "Amazon Redshift").

v6

- Added "About the Author". made site name in title a link, and made each chapter start a new page.
- Updated links to a mazonredshiftresearcproject.org to redshiftresearcproject.org.
- Reduced font size in tables where the numbers in the columns were overlapping.

v7

- $\bullet\,$ Web-site name changed to "Redshift Observatory".
- $\bullet~$ Updated links from redshift researcproject.org to redshift-observatory.ch.

v8

- Removed "About The Author".
- Added Slack join URL.

Appendix A: Raw Data Dump

Note these results are completely unprocessed; they are a raw dump of the results, so the original, wholly unprocessed data, is available.

```
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                                                                                                                           0.00035832533626134
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```

Appendix B: The Curious Step-Plan

So, the existing system tables are impossible to use and as such I've been developing a set of replacement system tables for a couple of years.

One of the views produces what I term a "step-plan". It's a bit like an EXPLAIN, except it tells the truth, but can only be used on a query which has completed. It's a list, in stream, segment and step order, per slice, of the steps which occurred, and some information about each one. So it's an actual, real listing of what a query really did. You'll see one shortly, in this appendix.

While I was working away on the investigation, one of the queries I issued is this:

```
insert into table_1 ( distribution_key, random_value )
select 0, random() from pg_class limit 5;
```

The idea is to get one leader-node query producing five rows, each with one random number, which then is written to a worker-node table.

Well, turns out that doesn't do what I thought it would, because *any* interaction with a worker-node means the worker nodes do the work, and so in this case, you end up with random numbers from the worker node PRNGs.

But the step-plan for this query is really remarkable, so much so I've made this appendix for it.

So here's what happens from the start up to the query;

```
dev=# create table table_1
dev-# (
dev(# distribution_key int2 not null encode raw distkey,
dev(# random_value float8 not null encode raw
dev(#)
dev-# diststyle key;
CREATE TABLE
dev=#
dev=# set seed = 0;
SET
dev=# insert into table_1 ( distribution_key, random_value ) select 0, random() from pg_cl
INSERT 0 5
```

dev=#

dev=# select random_value from table_1;
 random_value

- 0.892646380714737
- 0.579246389527981
- 0.462220476811851
- 0.743841628806479
- 0.363176232529966
- (5 rows)

Now for easy reference, here's the first ten numbers from the leader node PRNG, so we can see what we have up there in that table is from a worker node PRNG.

Value	,

 $\begin{array}{c} 0.840187716763467 \\ 0.394382926635444 \\ 0.783099223393947 \\ 0.798440033104271 \\ 0.911647357512265 \\ 0.197551369201392 \\ 0.335222755558789 \\ 0.768229594454169 \\ 0.277774710673839 \end{array}$

0.553969955537468

Now the step-plan.

dev=#							rows	bytes	start_time	duration	schematable_name	l notes
+						·	+		+		+	
520 I	0				12813		1835	0	2021-10-11 10:01:15			<u> </u>
520 I	0						1835		2021-10-11 10:01:15		<u> </u>	<u> </u>
520 I	0		2			distribute		0			<u> </u>	<u> </u>
520 I	0					scan	l 6 l	96	2021-10-11 10:01:15		<u> </u>	scan data from network to temp table
520 I	0 1						l 6 l	96	2021-10-11 10:01:15		l	scan data from network to temp table
520 I	0 1			1		scan	l 6 l	96	2021-10-11 10:01:15		l	scan data from network to temp table
520 I	0 1					scan	l 6 l	96	2021-10-11 10:01:15			scan data from network to temp table
520 I	0 1					limit	l 6 l		2021-10-11 10:01:15		l	
520 I	0 1					limit	l 6 l		2021-10-11 10:01:15		l	
520 I	0 1					limit	l 6 l		2021-10-11 10:01:15		I	
520 I	0 1					limit	l 6 l		2021-10-11 10:01:15		l	
520 I	0 1		2	0 1		return	l 5 l	80	2021-10-11 10:01:15		l	
520	0 1			0 1		return	l 5 l	80	2021-10-11 10:01:15		l	
520 I	0 1			1		return	l 5 l	80	2021-10-11 10:01:15		I	
520	0 1						l 5 l	80	2021-10-11 10:01:15		I	
520 I	0 1		0		12813		l 6 l	96	2021-10-11 10:01:15	0.000171	I	scan data from network to temp table
520 I	0 1				12813	limit	l 6 l		2021-10-11 10:01:15		I	I
520 I	0 1		2			project	5		2021-10-11 10:01:15	0.000171	I	I
520 I	0 1		3	I		project	5		2021-10-11 10:01:15	0.000171	I	I
520 I	0 1	2	6 I	I	12813	distribute	J 5 I	0	2021-10-11 10:01:15	0.000171	I	I
520 I	0 1	3	0	0 1	0	scan	I 0 I	0	2021-10-11 10:01:15	0.004097	I	scan data from network to temp table
520 I	0 1	3	0	0 1	1	scan	I 0 I	0	2021-10-11 10:01:15	0.004096	I	scan data from network to temp table
520 I	0 1	3	0	1	1 2	scan	I 0 I	0	2021-10-11 10:01:15	0.00508	I	scan data from network to temp table
520 I	0 1	3	0	1	J 3	scan	l 5 l	80	2021-10-11 10:01:15	0.00519	I	scan data from network to temp table
520 I	0 1	3	1	0 1	0	project	I 0 I		2021-10-11 10:01:15	0.004097	I	I
520 I	0 1	3	1	0 1	1	project	1 0 1		2021-10-11 10:01:15	0.004096	I	I
520 I	0 1	3	1	1	2	project	1 0 1		2021-10-11 10:01:15	0.00508	I	I
520 I	0 1	3	1	1	3	project	J 5 I		2021-10-11 10:01:15	0.00519	I	I
520 I	0 1	3	2	0 1	0	insert	1 0 1		2021-10-11 10:01:15	0.004097	public.table_1	I
520 I	0 1	3	2	0 1	1	insert	I 0 I		2021-10-11 10:01:15	0.004096	public.table_1	I
520 I	0 1	3	2	1	2	insert	1 0 1		2021-10-11 10:01:15	0.00508	public.table_1	I
520 I	0 1	3	2	1	3	insert	J 5 I		2021-10-11 10:01:15	0.00519	public.table_1	I
520 I	0 1	3	3	0 1	1 0	aggregate	1	8	2021-10-11 10:01:15	0.004097	I -	ungrouped, scalar aggregation in memory
520 I	0 1	3	3	0 1	1	aggregate	1	8	2021-10-11 10:01:15	0.004096	I	ungrouped, scalar aggregation in memory
520 I	0 1	3	3	1	1 2	aggregate	1	8	2021-10-11 10:01:15	0.00508	I	ungrouped, scalar aggregation in memory
520 I	0	3	3	1] 3	aggregate	1	8	2021-10-11 10:01:15	0.00519	ĺ	ungrouped, scalar aggregation in memory
520	1	4	0	0	0		1 1	8	2021-10-11 10:01:15	8.4e-05	I	scan data from temp table
520	1	4	0	0	1	scan	1 1	8	2021-10-11 10:01:15		i I	scan data from temp table
520	1	4	0	1	2	scan	1 1	8	2021-10-11 10:01:15	8.3e-05	i I	scan data from temp table
520 I	1	4	0 1	1	3	scan	. 1	8			İ	scan data from temp table

```
520 | 1 | 4 | 1 | 0 | 0 | return | 1 | 8 | 2021-10-11 10:01:15 | 8.4e-05 |
520 | 1 | 4 | 1 | 0 | 1 | return | 1 | 8 | 2021-10-11 10:01:15 | 3.4e-05 |
520 | 1 | 4 | 1 | 1 | 1 | 2 | return | 1 | 8 | 2021-10-11 10:01:15 | 3.6e-05 |
520 | 1 | 4 | 1 | 1 | 1 | 3 | return | 1 | 8 | 2021-10-11 10:01:15 | 8.3e-05 |
520 | 1 | 5 | 0 | 12813 | scan | 4 | 32 | 2021-10-11 10:01:15 | 7.8e-05 |
520 | 1 | 5 | 1 | 1 | 12813 | scan | 4 | 32 | 2021-10-11 10:01:15 | 0.001215 |
520 | 2 | 6 | 0 | 12813 | scan | 1 | 16 | 2021-10-11 10:01:15 | 0.001215 |
520 | 2 | 6 | 1 | 12813 | scan | 0 | 0 | 2021-10-11 10:01:15 | 4.3e-05 |
```

scan data from network to temp table ungrouped, scalar aggregation in memory scan data from temp table

Now, the first thing to node is the leader node has slice_id 12813 (at least in this query - it used to be leader node slice_id was always 6411, but now it seems (I've not investigated, so just offhand observations) to be a value starting at 12811 and varying by query).

So what happens first is the leader node reads all 1835 rows from pg_class, does not apply the limit clause, and distributes the rows to the worker nodes -but the number of bytes read is 0, and that makes sense, because no columns are read from pg_class.

All of the worker slices then scan six rows from the network (the distribution from the leader node in the previous step), and these six rows are 96 bytes in length.

This is fascinating.

First, why six? why not five? bug in the data, or is it really happening?

Second, we can see each row is 16 bytes in length, which is correct - one 8 byte timestamp, one 8 byte float8 - so it looks like the leader node has actually produced the timeofday() and the random() number. If it has, then it's done the work, and its sent the rows out the worker slices - but we know from inspecting the numbers in the table (as we know what numbers the leader node produces) we have PRNG output from the worker slices, not the leader node! and this implies the worker slice later overwrote the work done by the leader node!

The worker slices then apply the limit clause, and each returns 5 rows to the leader node (limit has to work this way, because none of the slices can know what the others returned, and all the others might have returned zero rows; but it's still a really useful thing to do because although the number of rows is still the limit value for every slice, that's still very likely to be a hell of a lot less than the *all* the rows).

We now return to the leader node, which scans - apparently - six rows from the network to a temp table.

I don't get this at all. I'd expect it to read 20 - 5 from each worker slice. Maybe it knows enough to apply the limit here? and the six is an off-by-one error?

We then see the actual limit step, getting us down to 5 rows, and then the project steps are for organizing columns, so not important for us here, and then the leader node again distributes the rows it has to the worker slices, this time for the insert.

The SQL has been arranged so all rows are going to be held on slice 3, so we see slices 0 to 2 have nothing, and slice 3 has all 5 rows and 80 bytes.

The insert then happens, and after that with the aggregate, scan and return, and the leader node processing, we're seeing the computation of how many rows each worker slice inserted, with this information being returned to the user.

Appendix C : Dieharder Results

There is a utility, dieharder, which applies a large range of statistical tests to PRNG output.

This is available on my Debian system from the Debian repository, but it's not necessarily available on other systems, and since the script which produces evidence for each white paper is specifically intended to be used by readers, I have not made it a dependency and so I have not included in the script the code I used to generate data for it.

I have however included the core code here (everything except the code which sets up a cluster and makes a connection).

I generated 10,000,000 32 bit values from the Python 3, leader node and worker slice 0 PRNGs, all from seed 0.

This was of course with a single query producing all values, as this is the working use case for Redshift.

To do with Redshift involves a slight element of uncertainty. The PRNG generates a value between 0.0 and 1.0, so it's not possible to know how many bits of random data are actually being generated by each call. I am then assuming it's at least 32 bits. If it's less, then the dieharder report will be invalid (as it is, given the PRNGs did well, it looks like it was okay).

Core Code

```
import array

print( 'Python PRNG data' )

random.seed( 0 )

data = []

for loop in range( 0, 10000000 ):
   data.append( random.randint(0, 4294967296) )

bf = array.array( 'L', data )

diskfile = open( 'prng_output_python.dat', 'wb' )

bf.tofile( diskfile )
```

```
diskfile.close()
print( 'Leader node PRNG data' )
issue_sql( connection_state, 'set seed = 0;' )
sql = 'select random() from pg_class as p1, pg_class as p2, pg_class as p3 limit 10000000;
rows, row_count = issue_sql( connection_state, sql )
data = []
for row in rows:
  data.append( int(row[0] * float(4294967296)) )
bf = array.array( 'L', data )
diskfile = open( 'prng_output_leader.dat', 'wb' )
bf.tofile( diskfile )
diskfile.close()
print( 'Worker node PRNG data' )
finished = False
while finished == False:
  issue_sql( connection_state, 'set seed = 0;' )
  sql = 'select slice_num(), random() from table_1 limit 10000000;'
  rows, row_count = issue_sql( connection_state, sql )
  if rows[0][0] == 0:
    data = []
    for row in rows:
      data.append( int(row[1] * float(4294967296)) )
    bf = array.array( 'L', data )
    diskfile = open( 'prng_output_worker.dat', 'wb' )
    bf.tofile( diskfile )
    diskfile.close()
    finished = True
```

Python 3.7.3

```
______
       dieharder version 3.31.1 Copyright 2003 Robert G. Brown
rng_name
                filename
                             |rands/second|
              prng_output_python.dat| 4.18e+07 |
   mt19937|
#-----#
    test_name | ntup | tsamples | psamples | p-value | Assessment
diehard birthdays | 0|
                   100|
                         100|0.91021316| PASSED
   diehard_operm5| 0|
                10000001
                         100|0.62391805| PASSED
 diehard_rank_32x32| 0|
                         100|0.86047849| PASSED
                  40000|
                         100|0.98245643| PASSED
  diehard_rank_6x8| 0|
                 100000|
 diehard_bitstream | 0 | 2097152 |
                         100|0.11901796| PASSED
    diehard_opso| 0| 2097152|
                        100|0.61501742| PASSED
```

```
diehard_oqso|
                            0|
                                  2097152
                                                 100 | 0.92247033 |
                                                                     PASSED
          diehard_dna|
                            0|
                                  2097152
                                                 100 | 0.98797513 |
                                                                     PASSED
diehard_count_1s_str|
                            0|
                                   256000|
                                                 100 | 0.56215375 |
                                                                     PASSED
diehard_count_1s_byt|
                            0|
                                   256000|
                                                 100 | 0.83967377 |
                                                                     PASSED
 diehard_parking_lot|
                            0|
                                    12000|
                                                 100 | 0.18735442 |
                                                                     PASSED
                            2|
    diehard 2dsphere
                                     10008
                                                 100 | 0.83203791 |
                                                                     PASSED
    diehard 3dsphere
                            3|
                                                                     PASSED
                                     4000|
                                                 100 | 0.92342130 |
     diehard_squeeze
                            01
                                   1000001
                                                 100 | 0.48740781 |
                                                                     PASSED
         diehard_sums|
                            01
                                                 100|0.76343976|
                                                                     PASSED
                                       100|
                            0|
         diehard_runs|
                                   100000|
                                                 100 | 0.54612314 |
                                                                     PASSED
         diehard_runs|
                            01
                                                                     PASSED
                                   100000|
                                                 100 | 0.81644432 |
       diehard_craps|
                            01
                                   2000001
                                                 100 | 0.48726638 |
                                                                     PASSED
       diehard_craps|
                            0|
                                   2000001
                                                 100|0.87719203|
                                                                     PASSED
marsaglia_tsang_gcd|
                            0|
                                 10000000|
                                                 100 | 0.10068775 |
                                                                     PASSED
marsaglia_tsang_gcd|
                            0|
                                 10000000|
                                                 100 | 0.68567671 |
                                                                     PASSED
                                                                     PASSED
          sts_monobit|
                                   100000|
                                                 100 | 0.38639892 |
                            1 |
              sts_runs|
                            21
                                   100000|
                                                 100 | 0.03197373 |
                                                                     PASSED
           sts_serial|
                            1|
                                   100000|
                                                 100 | 0.47083513 |
                                                                     PASSED
           sts serial
                            2|
                                   100000|
                                                 100 | 0.09539431 |
                                                                     PASSED
           sts_serial|
                            3|
                                                                     PASSED
                                   100000|
                                                 100 | 0.91055561 |
           sts_serial|
                            3|
                                   100000|
                                                 100 | 0.37027202 |
                                                                     PASSED
           sts_serial
                            4|
                                   100000|
                                                 100 | 0.85957342 |
                                                                     PASSED
           sts serial
                            4|
                                   100000|
                                                 100 | 0.74293426 |
                                                                     PASSED
           sts_serial|
                            5|
                                   100000|
                                                 100 | 0.26417245 |
                                                                     PASSED
                            5|
           sts_serial|
                                   100000|
                                                 100 | 0.98590100 |
                                                                     PASSED
           sts_serial|
                            6|
                                   100000|
                                                 100 | 0.50015357 |
                                                                     PASSED
           sts_serial|
                            6|
                                   100000|
                                                 100 | 0.23763476 |
                                                                     PASSED
                            7|
           sts_serial|
                                   1000001
                                                 100 | 0.27050504 |
                                                                     PASSED
           sts_serial|
                            7|
                                   100000|
                                                 100 | 0.06887525 |
                                                                     PASSED
           sts_serial|
                            8|
                                   100000|
                                                 100 | 0.37025966 |
                                                                     PASSED
           sts_serial|
                            81
                                   1000001
                                                 100 | 0.45902758 |
                                                                     PASSED
                            9|
                                                                     PASSED
           sts_serial|
                                   100000|
                                                 100|0.36453740|
           sts_serial|
                            9|
                                   100000|
                                                 100 | 0.47091905 |
                                                                     PASSED
           sts_serial|
                           10|
                                   100000|
                                                 100 | 0.13823639 |
                                                                     PASSED
           sts_serial|
                           10|
                                   100000 l
                                                 100 | 0.41825651 |
                                                                     PASSED
           sts_serial|
                           11|
                                   100000|
                                                 100 | 0.72056127 |
                                                                     PASSED
           sts_serial|
                           11|
                                   100000|
                                                 100 | 0.60510631 |
                                                                     PASSED
           sts serial
                                                                     PASSED
                           12|
                                   100000|
                                                 100 | 0.16750470 |
           sts_serial|
                                   100000I
                                                 100 | 0.08681430 |
                                                                     PASSED
                           12|
           sts_serial|
                           13|
                                   100000|
                                                 100 | 0.62165433 |
                                                                     PASSED
           sts_serial|
                           13|
                                   100000|
                                                 100 | 0.78142778 |
                                                                     PASSED
           sts_serial|
                           14|
                                   100000|
                                                 100 | 0.13083346 |
                                                                     PASSED
           sts_serial|
                           14|
                                   100000|
                                                 100|0.48723282|
                                                                     PASSED
           sts_serial|
                           15|
                                   100000|
                                                 100 | 0.69722467 |
                                                                     PASSED
           sts_serial|
                                   100000|
                                                 100 | 0.49267886 |
                                                                     PASSED
                           15 l
           sts_serial|
                           16|
                                   100000|
                                                 100 | 0.92524386 |
                                                                     PASSED
                                                                     PASSED
           sts_serial|
                           16|
                                   100000|
                                                 100 | 0.56477191 |
                                                                     PASSED
          rgb_bitdist|
                            1|
                                   100000|
                                                 100|0.65634586|
          rgb_bitdist|
                            2|
                                   1000001
                                                 100 | 0.49532436 |
                                                                     PASSED
          rgb_bitdist|
                            31
                                   100000|
                                                 100 | 0.47939635 |
                                                                     PASSED
```

```
100 | 0.21084338 |
                                                                    PASSED
                           41
                                   100000 I
          rgb_bitdist|
          rgb_bitdist|
                           5|
                                   1000001
                                                 100|0.08389079|
                                                                    PASSED
          rgb_bitdist|
                           6|
                                   100000|
                                                 100 | 0.98785894 |
                                                                    PASSED
          rgb_bitdist|
                           7|
                                   100000|
                                                 100 | 0.06729915 |
                                                                    PASSED
                           81
                                   100000|
                                                                      WEAK
          rgb_bitdist|
                                                 100 | 0.99625180 |
          rgb_bitdist|
                           9|
                                   100000|
                                                 100 | 0.31705621 |
                                                                    PASSED
          rgb bitdist
                                   100000I
                                                 100 | 0.72738052 |
                                                                    PASSED
                          10|
          rgb_bitdist|
                          11 l
                                   100000|
                                                 100 | 0.74987130 |
                                                                    PASSED
                          12|
                                   100000|
                                                 100 | 0.70277477 |
                                                                    PASSED
          rgb_bitdist|
                           2|
rgb_minimum_distance|
                                    10000|
                                               1000 | 0.20711437 |
                                                                    PASSED
                           3|
                                    10000|
                                               1000 | 0.95847441 |
                                                                    PASSED
rgb_minimum_distance
                           41
                                    10000|
                                               1000 | 0.73968906 |
                                                                    PASSED
{\tt rgb\_minimum\_distance}|
                                                                    PASSED
{\tt rgb\_minimum\_distance} \mid
                           5|
                                    10000|
                                               1000|0.26091900|
                           2|
                                   100000|
                                                 100 | 0.26802939 |
                                                                    PASSED
    rgb_permutations|
    rgb_permutations|
                           3|
                                   100000|
                                                 100 | 0.06202086 |
                                                                    PASSED
                           41
                                                                    PASSED
                                   100000 l
                                                 100 | 0.48429432 |
    rgb_permutations
                           5|
                                   100000|
                                                 100 | 0.15929449 |
                                                                    PASSED
    rgb_permutations
      rgb_lagged_sum|
                           0|
                                 1000000|
                                                 100 | 0.99843521 |
                                                                      WEAK
      rgb_lagged_sum|
                           1 |
                                 1000000|
                                                 100 | 0.40708004 |
                                                                    PASSED
      rgb_lagged_sum|
                           21
                                 10000001
                                                 100 | 0.52568156 |
                                                                    PASSED
                           3|
                                 1000000|
                                                                    PASSED
      rgb_lagged_sum|
                                                 100 | 0.84796544 |
                           4|
                                  1000000|
                                                 100 | 0.13148988 |
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                           5|
                                 1000000|
                                                 100 | 0.55538232 |
                                                                    PASSED
      rgb_lagged_sum|
                           6|
                                 1000000|
                                                 100 | 0.55227698 |
                                                                    PASSED
                           7|
      rgb_lagged_sum|
                                 1000000|
                                                 100|0.91975633|
                                                                    PASSED
                           81
                                 1000000|
                                                 100|0.84070991|
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                           9|
                                 1000000|
                                                 100|0.48917896|
                                                                    PASSED
                          101
                                 1000000|
                                                 100 | 0.22535359 |
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                          11 l
                                 1000000|
                                                 100 | 0.14795671 |
                                                                    PASSED
                          12|
                                 1000000|
                                                 100 | 0.96211921 |
                                                                    PASSED
      rgb_lagged_sum|
                          13|
                                 1000000|
                                                 100 | 0.96644383 |
                                                                    PASSED
      rgb_lagged_sum|
                          14|
                                                                    PASSED
                                 1000000|
                                                 100 | 0.48127863 |
      rgb_lagged_sum|
      rgb_lagged_sum|
                          15|
                                 1000000|
                                                 100 | 0.28678048 |
                                                                    PASSED
      rgb_lagged_sum|
                          16|
                                 1000000|
                                                 100 | 0.94131471 |
                                                                    PASSED
      rgb_lagged_sum|
                          17|
                                 1000000|
                                                 100 | 0.98791186 |
                                                                    PASSED
                                                                    PASSED
                          18 l
                                 1000000|
                                                 100 | 0.52883737 |
      rgb_lagged_sum|
      rgb_lagged_sum|
                          19|
                                 1000000|
                                                 100|0.98808888|
                                                                    PASSED
                                 1000000|
                                                 100 | 0.74873563 |
                                                                    PASSED
      rgb_lagged_sum|
                          20 I
      rgb_lagged_sum|
                          21 l
                                 10000001
                                                 100 | 0.49714591 |
                                                                    PASSED
                          22|
                                 1000000|
                                                 100|0.46740536|
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                          23|
                                 1000000|
                                                 100 | 0.17966965 |
                                                                    PASSED
      rgb_lagged_sum|
                          24|
                                 1000000|
                                                 100 | 0.95621705 |
                                                                    PASSED
                          251
                                 1000000|
                                                 100 | 0.53383031 |
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                          26|
                                 1000000|
                                                 100 | 0.07479719 |
                                                                    PASSED
                                  1000000|
                                                 100 | 0.75256734 |
                                                                    PASSED
      rgb_lagged_sum|
                          27 I
      rgb_lagged_sum|
                          28|
                                 1000000|
                                                 100 | 0.63078770 |
                                                                    PASSED
                                                                    PASSED
                          29|
                                 10000001
                                                 100 | 0.94394862 |
      rgb_lagged_sum|
                          30|
                                                                    PASSED
      rgb_lagged_sum|
                                 1000000|
                                                 100|0.85699054|
                          31|
                                 1000000|
                                                 100 | 0.24538772 |
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                          321
                                 1000000|
                                                 100 | 0.55014932 |
                                                                    PASSED
```

```
100001
                                          1000|0.08125982|
                                                             PASSED
     rgb_kstest_test|
                        01
     dab_bytedistrib|
                        0|
                            51200000
                                             1|0.21319946|
                                                             PASSED
             dab_dct| 256|
                               50000|
                                             1|0.11947066|
                                                             PASSED
Preparing to run test 207.
                             ntuple = 0
        dab_filltree|
                             15000000|
                       32|
                                             1|0.53754123|
                                                             PASSED
        dab filltree
                             15000000|
                                             1|0.46607264|
                                                             PASSED
                       32|
Preparing to run test 208.
                             ntuple = 0
                              50000001
                                                             PASSED
       dab_filltree2|
                         01
                                             1 | 0.08515787 |
       dab_filltree2|
                         1|
                              50000001
                                             1|0.57370950|
                                                             PASSED
Preparing to run test 209.
                             ntuple = 0
        dab_monobit2 | 12 |
                             650000001
                                             1|0.88376526|
                                                             PASSED
```

Redshift Leader Node (dc2.large, 2 nodes, 1.0.30840)

```
#-----#
           dieharder version 3.31.1 Copyright 2003 Robert G. Brown
                                                                   =====#
  _____
  rng_name
                        filename
                                            |rands/second|
                       prng_output_leader.dat| 8.64e+07
       mt19937|
                  |ntup| tsamples | psamples | p-value | Assessment
       test_name
100|0.56283496| PASSED
  diehard_birthdays|
                      0|
                              100|
     diehard_operm5|
                      0|
                          1000000|
                                      100|0.78028660|
                                                      PASSED
 diehard_rank_32x32|
                     01
                            40000 l
                                      100|0.08944208|
                                                     PASSED
   diehard rank 6x8|
                      0|
                           100000|
                                      100 | 0.00439802 |
                                                       WEAK
  diehard bitstream
                          2097152|
                                      100|0.13079436|
                                                     PASSED
                      01
       diehard_opso|
                      01
                          2097152
                                      100|0.02301681| PASSED
       diehard_oqso|
                      0|
                          2097152
                                      100|0.20625063|
                                                      PASSED
        diehard_dna|
                      0|
                          2097152
                                      100 | 0.70311401 |
                                                      PASSED
diehard_count_1s_str|
                           256000|
                                      100|0.88127953|
                                                      PASSED
diehard_count_1s_byt|
                      01
                           2560001
                                      100|0.94238111|
                                                      PASSED
                      0|
                            12000|
                                                      PASSED
diehard_parking_lot|
                                      100|0.77995133|
                      21
   diehard_2dsphere|
                            8000
                                      100 | 0.99544227 |
                                                       WEAK
   diehard_3dsphere|
                                                      PASSED
                             4000|
                                      100|0.97261935|
    diehard_squeeze|
                      01
                           100000|
                                                      PASSED
                                      100 | 0.24671327 |
       diehard_sums|
                      01
                                                      PASSED
                              100|
                                      100|0.24126608|
       diehard_runs|
                      01
                           100000|
                                      100|0.92369114|
                                                      PASSED
       diehard_runs|
                           100000|
                                      100 | 0.28035254 |
                                                      PASSED
                      01
                           200000|
      diehard_craps|
                                      100|0.62306358|
                                                      PASSED
      diehard_craps|
                      0|
                           2000001
                                      100 | 0.65024299 |
                                                      PASSED
marsaglia_tsang_gcd|
                         10000000|
                                      100|0.34694024|
                                                      PASSED
marsaglia_tsang_gcd|
                      0|
                         10000000|
                                      100 | 0.30239745 |
                                                      PASSED
        sts_monobit|
                           100000|
                                      100|0.82007359|
                                                      PASSED
                      11
           sts_runs|
                      2|
                           100000|
                                      100|0.84952560|
                                                      PASSED
         sts serial|
                           100000|
                                      100 | 0.61632763 |
                                                      PASSED
                      11
         sts serial|
                      21
                           1000001
                                      100|0.25207783| PASSED
```

```
100 | 0.99652792 |
           sts_serial |
           sts_serial|
                            3|
                                   100000|
                                                 100 | 0.34499257 |
                                                                     PASSED
           sts_serial|
                            4|
                                   100000|
                                                 100|0.83698688|
                                                                     PASSED
           sts_serial|
                            41
                                   100000|
                                                 100|0.54069181|
                                                                     PASSED
           sts_serial|
                            5|
                                                                     PASSED
                                   100000 l
                                                 100 | 0.13307143 |
           sts serial
                            5|
                                   100000|
                                                 100 | 0.00435777 |
                                                                      WEAK
           sts serial
                                                                     PASSED
                            6|
                                   100000|
                                                 100 | 0.45527377 |
           sts_serial|
                            61
                                   1000001
                                                 100 | 0.01378227 |
                                                                     PASSED
                            7|
                                   1000001
                                                                     PASSED
           sts_serial|
                                                 100 | 0.86954268 |
                            7|
           sts_serial|
                                   100000|
                                                 100 | 0.92394266 |
                                                                     PASSED
                            8|
                                                                     PASSED
           sts_serial|
                                   100000|
                                                 100 | 0.96815681 |
                            81
                                   100000|
                                                 100 | 0.73415977 |
           sts_serial|
                                                                     PASSED
           sts_serial|
                            9|
                                   100000|
                                                 100|0.59889026|
                                                                     PASSED
           sts_serial|
                            9|
                                   100000|
                                                 100 | 0.83489705 |
                                                                     PASSED
           sts_serial|
                           10|
                                   100000|
                                                 100 | 0.26949493 |
                                                                     PASSED
                                                                     PASSED
           sts_serial|
                           10|
                                   100000 l
                                                 100 | 0.04740705 |
           sts_serial|
                                   100000|
                                                 100 | 0.66772942 |
                                                                     PASSED
                           11|
           sts_serial|
                           11|
                                   100000|
                                                 100 | 0.84818719 |
                                                                     PASSED
           sts serial|
                           12|
                                   100000|
                                                 100 | 0.47073317 |
                                                                     PASSED
           sts_serial|
                                   1000001
                                                                     PASSED
                           12|
                                                 100 | 0.21470601 |
           sts_serial|
                                                                     PASSED
                           13|
                                   100000 l
                                                 100 | 0.20460068 |
           sts_serial|
                           13|
                                   100000|
                                                 100 | 0.47596139 |
                                                                     PASSED
           sts_serial|
                           14|
                                   100000|
                                                 100 | 0.45279396 |
                                                                     PASSED
           sts_serial|
                           14|
                                   100000|
                                                 100 | 0.63986527 |
                                                                     PASSED
           sts_serial|
                           15|
                                   100000|
                                                 100 | 0.86743415 |
                                                                     PASSED
           sts_serial|
                           15|
                                   100000|
                                                 100|0.99189999|
                                                                     PASSED
           sts_serial |
                           16|
                                   100000|
                                                 100 | 0.38905282 |
                                                                     PASSED
                           16|
                                   100000|
                                                                     PASSED
           sts_serial|
                                                 100 | 0.92489209 |
          rgb_bitdist|
                            1|
                                   100000|
                                                 100 | 0.16886848 |
                                                                     PASSED
          rgb_bitdist|
                            2|
                                   100000|
                                                 100 | 0.61718315 |
                                                                     PASSED
          rgb_bitdist|
                            31
                                   1000001
                                                 100 | 0.95878298 |
                                                                     PASSED
                            4|
                                                                     PASSED
          rgb_bitdist|
                                   100000|
                                                 100 | 0.15758441 |
          rgb_bitdist|
                            5|
                                   100000|
                                                 100 | 0.68642455 |
                                                                     PASSED
          rgb_bitdist|
                            6|
                                   100000|
                                                 100 | 0.98846650 |
                                                                     PASSED
          rgb_bitdist|
                            7|
                                   1000001
                                                 100 | 0.77423360 |
                                                                     PASSED
                            81
          rgb_bitdist|
                                   100000|
                                                 100 | 0.07418954 |
                                                                     PASSED
          rgb_bitdist|
                            9|
                                   100000|
                                                 100 | 0.27655315 |
                                                                     PASSED
          rgb bitdist
                                                                     PASSED
                           10|
                                   100000|
                                                 100 | 0.36952839 |
          rgb_bitdist|
                                   1000001
                                                 100 | 0.90331503 |
                                                                     PASSED
                           111
          rgb_bitdist|
                           12|
                                   100000|
                                                 100 | 0.76369571 |
                                                                     PASSED
rgb_minimum_distance|
                            2|
                                    10000|
                                                1000 | 0.90089954 |
                                                                     PASSED
rgb_minimum_distance|
                            3|
                                    10000|
                                                1000 | 0.71580309 |
                                                                     PASSED
rgb_minimum_distance|
                            41
                                    10000|
                                                1000 | 0.89880503 |
                                                                     PASSED
rgb_minimum_distance
                            5|
                                    10000|
                                                1000|0.38681646|
                                                                     PASSED
    rgb_permutations|
                            2|
                                   100000|
                                                 100 | 0.38359949 |
                                                                     PASSED
    rgb_permutations|
                            3|
                                   100000|
                                                 100 | 0.99333476 |
                                                                     PASSED
                            41
                                                                     PASSED
                                   100000|
                                                 100|0.84905096|
    rgb_permutations
                            5|
                                                                     PASSED
    rgb_permutations|
                                   100000|
                                                 100|0.38148715|
       rgb_lagged_sum|
                            01
                                  10000001
                                                 100 | 0.06409286 |
                                                                     PASSED
      rgb_lagged_sum|
                            1|
                                  1000000|
                                                 100 | 0.80057461 |
                                                                     PASSED
```

3|

100000|

WF.AK

```
PASSED
      rgb_lagged_sum|
                           2|
                                10000001
                                               100 | 0.09333652 |
      rgb_lagged_sum|
                           31
                                1000000|
                                               100|0.91841324|
                                                                  PASSED
      rgb_lagged_sum|
                           41
                                1000000|
                                               100 | 0.99895328 |
                                                                   WEAK
      rgb_lagged_sum|
                           5|
                                1000000|
                                               100 | 0.49388161 |
                                                                  PASSED
      rgb_lagged_sum|
                           61
                                                                  PASSED
                                1000000|
                                               100 | 0.93171221 |
                           7|
      rgb_lagged_sum|
                                1000000|
                                               100 | 0.37124762 |
                                                                  PASSED
      rgb lagged sum
                           81
                                10000001
                                               100 | 0.20428193 |
                                                                  PASSED
      rgb_lagged_sum|
                           91
                                1000000|
                                               100 | 0.57891575 |
                                                                  PASSED
                         10|
                                1000000|
                                               100|0.99323346|
                                                                  PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                          11|
                                1000000|
                                               100 | 0.17333651 |
                                                                  PASSED
                          12|
                                                                  PASSED
      rgb_lagged_sum|
                                1000000|
                                               100 | 0.46028373 |
      rgb_lagged_sum|
                         13|
                                1000000|
                                               100 | 0.27928022 |
                                                                  PASSED
      rgb_lagged_sum|
                          14|
                                1000000|
                                               100|0.00015476|
                                                                   WEAK
      rgb_lagged_sum|
                          15|
                                1000000|
                                               100 | 0.16088120 |
                                                                  PASSED
                                                                  PASSED
      rgb_lagged_sum|
                         16|
                                1000000|
                                               100 | 0.82912224 |
      rgb_lagged_sum|
                         17|
                                                                  PASSED
                                10000001
                                               100 | 0.76751496 |
      rgb_lagged_sum|
                         18|
                                1000000|
                                               100 | 0.09242822 |
                                                                  PASSED
      rgb_lagged_sum|
                         19|
                                1000000|
                                               100 | 0.81326560 |
                                                                  PASSED
      rgb_lagged_sum|
                         201
                                1000000|
                                               100 | 0.98568170 |
                                                                  PASSED
                         211
                                10000001
                                                                  PASSED
      rgb_lagged_sum|
                                               100 | 0.86151519 |
                         22|
                                                                  PASSED
      rgb_lagged_sum|
                                1000000|
                                               100|0.28338323|
      rgb_lagged_sum|
                         23|
                                1000000|
                                               100 | 0.41254617 |
                                                                  PASSED
      rgb_lagged_sum|
                         24|
                                1000000|
                                               100 | 0.85047392 |
                                                                  PASSED
      rgb_lagged_sum|
                         25|
                                1000000|
                                               100 | 0.76482908 |
                                                                  PASSED
      rgb_lagged_sum|
                         26|
                                1000000|
                                               100|0.24530833|
                                                                  PASSED
      rgb_lagged_sum|
                         27|
                                1000000|
                                               100|0.09792350|
                                                                  PASSED
      rgb_lagged_sum|
                         28|
                                1000000|
                                               100|0.98778393|
                                                                  PASSED
                         291
                                1000000|
                                               100 | 0.10214293 |
                                                                  PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                         301
                                1000000|
                                               100 | 0.36574781 |
                                                                  PASSED
      rgb_lagged_sum|
                         31|
                                1000000|
                                               100 | 0.71726766 |
                                                                  PASSED
      rgb_lagged_sum|
                         321
                                1000000|
                                               100 | 0.08671454 |
                                                                  PASSED
     rgb_kstest_test|
                           01
                                                                  PASSED
                                   10000|
                                              1000|0.26474364|
     dab_bytedistrib|
                           0|
                               51200000|
                                                 1|0.81035173|
                                                                  PASSED
              dab_dct| 256|
                                  50000|
                                                 1|0.90913523|
                                                                  PASSED
Preparing to run test 207.
                               ntuple = 0
        dab_filltree|
                               15000000|
                                                 1|0.73063369|
                                                                  PASSED
                         32|
                                                                  PASSED
        dab_filltree|
                         32|
                               15000000|
                                                 1|0.42227581|
Preparing to run test 208.
                               ntuple = 0
       dab filltree2|
                           01
                                5000000I
                                                 110.080318041
                                                                  PASSED
       dab_filltree2|
                           1 |
                                5000000|
                                                 1|0.46052720|
                                                                  PASSED
Preparing to run test 209.
                               ntuple = 0
         dab monobit2
                        12|
                               65000000|
                                                 1|0.32862265|
                                                                  PASSED
```

Redshift Worker Slice 0 (dc2.large, 2 nodes, 1.0.30840)

#-----#

dieharder version 3.31.1 Copyright 2003 Robert G. Brown #

```
rng_name
                           filename
                                                 |rands/second|
       mt19937|
                          prng_output_worker.dat| 7.35e+07
#-----
                    |ntup| tsamples |psamples| p-value |Assessment
        test_name
100|0.98552888|
  diehard birthdays
                                                            PASSED
                                 100 l
      diehard_operm5|
                        01
                             1000000|
                                           100 | 0.23622484 |
                                                            PASSED
  diehard_rank_32x32|
                        01
                               40000|
                                                            PASSED
                                           100 | 0.41156151 |
                        01
   diehard_rank_6x8|
                              100000|
                                           100 | 0.26737892 |
                                                            PASSED
  diehard_bitstream |
                        01
                             2097152|
                                           100 | 0.28538664 |
                                                            PASSED
        diehard_opso|
                        01
                             2097152
                                           100 | 0.84712054 |
                                                            PASSED
        diehard_oqso|
                        0|
                             2097152
                                           100|0.87412791|
                                                            PASSED
         diehard_dna|
                        0|
                             2097152|
                                           100 | 0.85570330 |
                                                            PASSED
diehard_count_1s_str|
                        0|
                              256000|
                                           100|0.37831511|
                                                            PASSED
diehard_count_1s_byt|
                        01
                                                            PASSED
                              2560001
                                           100 | 0.70217420 |
diehard_parking_lot|
                        01
                               12000
                                           100|0.98448969|
                                                            PASSED
   diehard_2dsphere
                        2|
                                10008
                                           100 | 0.83764169 |
                                                            PASSED
   diehard 3dsphere
                        31
                                4000|
                                           100 | 0.16493064 |
                                                            PASSED
     diehard_squeeze|
                        01
                              1000001
                                           100 | 0.46299607 |
                                                            PASSED
        diehard_sums|
                        0|
                                           100 | 0.02395836 |
                                                            PASSED
                                 100 l
        diehard_runs|
                        0|
                              100000|
                                           100 | 0.72829432 |
                                                            PASSED
        diehard runs
                        0|
                              100000|
                                           100 | 0.90137611 |
                                                            PASSED
       diehard_craps|
                        01
                              200000
                                           100 | 0.02756788 |
                                                            PASSED
       diehard_craps|
                        0|
                              2000001
                                           100|0.76981361|
                                                            PASSED
marsaglia_tsang_gcd|
                        0|
                            10000000|
                                           100|0.92486587|
                                                            PASSED
marsaglia_tsang_gcd|
                        0|
                            10000000|
                                           100|0.82768046|
                                                            PASSED
         sts_monobit|
                        1 |
                              100000|
                                           100|0.64653275|
                                                            PASSED
            sts_runs|
                        2|
                              100000|
                                           100 | 0.30846507 |
                                                            PASSED
          sts_serial|
                        1|
                              1000001
                                           100 | 0.88152740 |
                                                            PASSED
          sts_serial |
                        21
                              1000001
                                           100 | 0.99979017 |
                                                             WEAK
                        3|
                                                            PASSED
          sts_serial |
                              1000001
                                           100 | 0.58904454 |
          sts_serial|
                        3|
                               100000|
                                           100 | 0.61237276 |
                                                            PASSED
          sts_serial|
                        4|
                               100000|
                                           100 | 0.10318355 |
                                                            PASSED
          sts_serial |
                        41
                              100000|
                                           100|0.23471200|
                                                            PASSED
          sts_serial|
                        5|
                                                            PASSED
                              1000001
                                           100 | 0.14776957 |
                        5|
          sts_serial|
                              100000|
                                           100 | 0.94426624 |
                                                            PASSED
          sts serial
                        6|
                              100000|
                                           100 | 0.43325597 |
                                                            PASSED
          sts serial|
                        61
                              1000001
                                           100 | 0.32473662 |
                                                            PASSED
          sts_serial|
                        7|
                              100000|
                                           100|0.46231799|
                                                            PASSED
                        7|
          sts_serial |
                              100000|
                                           100 | 0.57226154 |
                                                            PASSED
          sts serial
                        81
                              100000|
                                           100 | 0.75570832 |
                                                            PASSED
                        81
          sts_serial |
                              1000001
                                           100 | 0.63532223 |
                                                            PASSED
          sts_serial|
                        9|
                              100000|
                                           100|0.41982537|
                                                            PASSED
          sts_serial|
                        9|
                              100000|
                                           100 | 0.02958411 |
                                                            PASSED
          sts_serial|
                       10|
                              100000|
                                           100 | 0.55335691 |
                                                            PASSED
                       10|
                                           100|0.29778251|
                                                            PASSED
          sts_serial|
                              1000001
                              100000|
                                                            PASSED
          sts_serial|
                       11|
                                           100|0.89033787|
          sts_serial |
                       11|
                               1000001
                                           100 | 0.69445886 |
                                                            PASSED
          sts_serial|
                       12|
                               100000|
                                           100 | 0.70028280 |
                                                            PASSED
```

```
100|0.37050033|
                                                                    PASSED
                          12|
                                   100000 I
           sts_serial|
           sts_serial|
                          13|
                                   1000001
                                                 100 | 0.82209080 |
                                                                    PASSED
           sts_serial |
                          13|
                                   100000|
                                                 100 | 0.19545550 |
                                                                    PASSED
           sts_serial|
                          14|
                                   100000|
                                                 100 | 0.25804521 |
                                                                    PASSED
           sts_serial|
                          14|
                                   100000|
                                                 100|0.80358025|
                                                                    PASSED
           sts serial
                          15|
                                   100000|
                                                 100 | 0.89065155 |
                                                                    PASSED
           sts serial
                                   100000I
                                                 100 | 0.98312073 |
                                                                    PASSED
                          15|
           sts_serial |
                          16|
                                   1000001
                                                 100 | 0.27731748 |
                                                                    PASSED
           sts_serial|
                          16|
                                   100000|
                                                 100 | 0.51880516 |
                                                                    PASSED
          rgb_bitdist|
                           1|
                                   100000|
                                                 100 | 0.20214026 |
                                                                    PASSED
                           2|
                                   100000|
                                                 100 | 0.17699662 |
                                                                    PASSED
          rgb_bitdist|
                           31
                                   100000|
                                                 100 | 0.69509415 |
                                                                    PASSED
          rgb_bitdist|
          rgb_bitdist|
                           4|
                                   100000|
                                                 100|0.65004993|
                                                                    PASSED
          rgb_bitdist|
                           5|
                                   100000|
                                                 100 | 0.99160017 |
                                                                    PASSED
          rgb_bitdist|
                           6|
                                   100000|
                                                 100 | 0.81048325 |
                                                                    PASSED
                           7|
                                                 100|0.97492388|
                                                                    PASSED
          rgb_bitdist|
                                   100000 l
          rgb_bitdist|
                           81
                                   100000|
                                                 100 | 0.58948307 |
                                                                    PASSED
          rgb_bitdist|
                           9|
                                   100000|
                                                 100 | 0.46751274 |
                                                                    PASSED
          rgb bitdist|
                          10|
                                   100000|
                                                 100 | 0.89638556 |
                                                                    PASSED
          rgb_bitdist|
                                   1000001
                                                                    PASSED
                          11|
                                                 100 | 0.52860331 |
          rgb_bitdist|
                          12|
                                   100000|
                                                                    PASSED
                                                 100 | 0.03558371 |
rgb_minimum_distance
                           2|
                                    10000|
                                               1000 | 0.37767141 |
                                                                    PASSED
rgb_minimum_distance|
                           3|
                                    10000|
                                               1000 | 0.16219517 |
                                                                    PASSED
rgb_minimum_distance|
                           41
                                    10000|
                                               1000 | 0.88737620 |
                                                                    PASSED
                           5|
rgb_minimum_distance|
                                    10000|
                                               1000|0.04465040|
                                                                    PASSED
    rgb_permutations|
                           2|
                                   100000|
                                                 100 | 0.99236354 |
                                                                    PASSED
                           3|
    rgb_permutations|
                                   100000|
                                                 100 | 0.52719628 |
                                                                    PASSED
                           41
                                   100000|
                                                 100 | 0.76115210 |
                                                                    PASSED
    rgb_permutations|
    rgb_permutations
                           5|
                                   100000|
                                                 100 | 0.73836345 |
                                                                    PASSED
                           01
                                 1000000|
                                                 100 | 0.29463994 |
                                                                    PASSED
       rgb_lagged_sum|
       rgb_lagged_sum|
                           1|
                                 1000000|
                                                 100 | 0.10403868 |
                                                                    PASSED
                           2|
                                                                    PASSED
      rgb_lagged_sum|
                                 1000000|
                                                 100 | 0.79554102 |
      rgb_lagged_sum|
                           3|
                                 1000000|
                                                 100 | 0.99019672 |
                                                                    PASSED
      rgb_lagged_sum|
                           4|
                                 1000000|
                                                 100 | 0.87160049 |
                                                                    PASSED
      rgb_lagged_sum|
                           51
                                 1000000|
                                                 100 | 0.63526097 |
                                                                    PASSED
                                                                    PASSED
                           61
                                 1000000|
                                                 100 | 0.78164429 |
      rgb_lagged_sum|
                           7|
      rgb_lagged_sum|
                                 1000000|
                                                 100 | 0.01414177 |
                                                                    PASSED
                           81
                                 1000000|
                                                                    PASSED
      rgb lagged sum
                                                 100 | 0.91120273 |
      rgb_lagged_sum|
                           91
                                 10000001
                                                 100 | 0.56019077 |
                                                                    PASSED
      rgb_lagged_sum|
                          10|
                                 1000000|
                                                 100|0.88819428|
                                                                    PASSED
      rgb_lagged_sum|
                          11|
                                 1000000|
                                                 100 | 0.13060075 |
                                                                    PASSED
      rgb_lagged_sum|
                          12|
                                 1000000|
                                                 100 | 0.28264461 |
                                                                    PASSED
                          131
                                 1000000|
                                                 100 | 0.44541582 |
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                          14 l
                                 1000000|
                                                 100 | 0.29494481 |
                                                                    PASSED
                          15|
                                 1000000|
                                                 100 | 0.33588815 |
                                                                    PASSED
      rgb_lagged_sum|
      rgb_lagged_sum|
                          16|
                                 1000000|
                                                 100 | 0.55206878 |
                                                                    PASSED
                          17|
                                                                    PASSED
                                 10000001
                                                 100 | 0.75623644 |
      rgb_lagged_sum|
                          18|
                                                                    PASSED
      rgb_lagged_sum|
                                 1000000|
                                                 100|0.80892139|
      rgb_lagged_sum|
                          19|
                                 10000001
                                                 100 | 0.98600606 |
                                                                    PASSED
      rgb_lagged_sum|
                          201
                                 1000000|
                                                 100 | 0.32999864 |
                                                                    PASSED
```

rgb_lagged_sum 21	1000000	100 0.60481492	PASSED
rgb_lagged_sum 22	1000000	100 0.91392204	PASSED
rgb_lagged_sum 23	1000000	100 0.93116828	PASSED
rgb_lagged_sum 24	1000000	100 0.09761773	PASSED
rgb_lagged_sum 25	1000000	100 0.94670973	PASSED
rgb_lagged_sum 26	1000000	100 0.14857654	PASSED
rgb_lagged_sum 27	1000000	100 0.17125207	PASSED
rgb_lagged_sum 28	1000000	100 0.44112337	PASSED
rgb_lagged_sum 29	1000000	100 0.37278694	PASSED
rgb_lagged_sum 30	1000000	100 0.02877012	PASSED
rgb_lagged_sum 31	1000000	100 0.56022772	PASSED
rgb_lagged_sum 32	1000000	100 0.20013696	PASSED
rgb_kstest_test 0	10000	1000 0.42363767	PASSED
dab_bytedistrib 0	51200000	1 0.32558216	PASSED
dab_dct 256	50000	1 0.40829491	PASSED
Preparing to run test 207	. ntuple = 0		
dab_filltree 32	15000000	1 0.15439468	PASSED
dab_filltree 32	15000000	1 0.97294404	PASSED
Preparing to run test 208	. ntuple = 0		
dab_filltree2 0	5000000	1 0.65211516	PASSED
dab_filltree2 1	5000000	1 0.00399712	WEAK
Preparing to run test 209	. ntuple = 0		
dab_monobit2 12	65000000	1 0.49219072	PASSED

Summary

Python was weak for the following tests;

rgb_bitdist	8	100000	100 0.99625180	WEAK
rgb_lagged_sum	0	1000000	100 0.99843521	WEAK

The leader node was weak for the following tests;

diehard_rank_6x8	0	100000	100 0.00439802	WEAK
diehard_2dsphere	2	8000	100 0.99544227	WEAK
sts_serial	3	100000	100 0.99652792	WEAK
sts_serial	5	100000	100 0.00435777	WEAK
rgb_lagged_sum	4	1000000	100 0.99895328	WEAK
rgb_lagged_sum	14	1000000	100 0.00015476	WEAK

Worker slice 0 was weak for the following tests;

sts_serial	2	100000	100 0.99979017	WEAK
dab filltree2	1	50000001	1 0.00399712	WEAK

Redshift Observatory Slack

I've started up a Redshift Slack.

Join URL is;

https://join.slack.com/t/redshift $observatory/shared_invite/zt-2vm3deqis-hc6h4GMDcG6Gs7\sim IECQNuQ$